M. Ben Amar

ICFP COURSE: Morphogenesis

A continuous viewpoint of morphogenesis.

Preliminaries: : This plan takes into account the advancement in the Stephan Fauve's course in the technics of nonlinear physics

1 Chemical dynamical systems and patterns formation.

- 1a) Chemical reactions, law of mass action, singular perturbation analysis.
- 1b) Mass-flux equation and reaction-diffusion equations: The Turing Instabil- ity.
- **1c)** Mass-flux equation for biological systems: chemotaxis, haptotaxis... *Nonlinear physics tools*: Boundary layer, linear stability analysis.

2 Biochemical signaling and mechanics.

- 2a) From cells to tissues. Introduction to elasticity and visco-elasticity.
- 2b) Activity or how to modify the mechanical laws.
- 2c) The mixture model and tumor growth.
- **2d)** The theory of active gels.

Nonlinear physics tools: Variational techniques, self-similar solutions

3 Morphogenesis of Physical systems.

- 3a) Viscous fingering and dendritic growth: model systems for growth in physics and free-boundary problems.
- **3b)** Volume equation and boundary conditions of Dirichlet and Neumann types.
- **3c)** Elementary solutions: the planar and radial front solutions analysis. From viscous fingering to fractal growth.
- **3d)** Exact soltions. Capillarity as a selection parameter. WKB methods. *Nonlinear physics tools*: Neumann boundary conditions with sources, com- plex analysis, selection

4 Free-boundary problems and living colonies.

- **4a)** Fluid colonies of bacteria (active or passive)
- **4b)** Moving epithelia on solid substrate: chemotaxis, durotaxis and homeosta-sis. *Nonlinear physics tools*: Galilean invariance, Normal Form